

# Sine Waves

*Drawing Mathematics with Desmos | Justin Skycak*

**Setup.** Navigate to <https://www.desmos.com/calculator>. Be sure to sign in so that you can save your graph.

**Demonstration - Equilibrium.** Observe the graph as you type each of the following inputs. In general, the graph of  $y = \sin x$  looks like an infinite wavy squiggle oscillating up and down around an equilibrium at  $y = 0$ . The graph  $y = \sin(x) + b$  shifts the equilibrium of the wavy squiggle to the line  $y = b$ .

$$y = \sin(x) + 5$$

$$y = \sin(x) + 1$$

$$y = \sin(x) + 0$$

$$y = \sin(x) - 1$$

$$y = \sin(x) - 5$$

**Demonstration - Frequency.** Observe the graph as you type each of the following inputs. The “frequency” of a sine wave refers to how quickly or “frequently” it oscillates. For a sine wave  $y = \sin(vx)$ , the frequency is controlled by  $v$ . If you double  $v$ , then the sine wave will oscillate twice as frequently; if you halve  $v$ , then the sine

wave will oscillate half as frequently. If you set  $v = 0$ , then the sine wave will not oscillate at all.

$$y = \sin(x)$$

$$y = \sin(2x)$$

$$y = \sin(4x)$$

$$y = \sin(x)$$

$$y = \sin(0.5x)$$

$$y = \sin(0.25x)$$

**Demonstration - Amplitude.** Observe the graph as you type each of the following inputs. The “amplitude” of a sine wave refers to how high/low its peaks/valleys are in relation to its equilibrium. For a sine wave  $y = A \sin(x)$ , the amplitude is controlled by  $A$ . The peaks of the sine wave reach a height of  $A$ , and the valleys of the sine wave reach a depth of  $-A$ .

$$y = 5 \sin(x)$$

$$y = 1 \sin(x)$$

$$y = 0.25 \sin(x)$$

**Demonstration - Horizontal Shift.** Observe the graph as you type each of the following inputs. The sine graph  $y = \sin(x - a)$  is shifted right  $a$  units, meaning that each peak and each valley occurs  $a$  units right of its original location.

$$y = \sin(x)$$

$$y = \sin(x - 1)$$

$$y = \sin(x - 1.57)$$

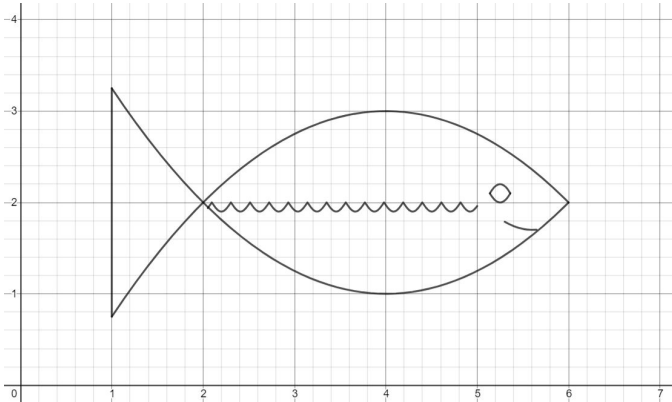
$$y = \sin(x - 2)$$

**Demonstration - Composition with Absolute Value.** Observe the graph as you type each of the following inputs.

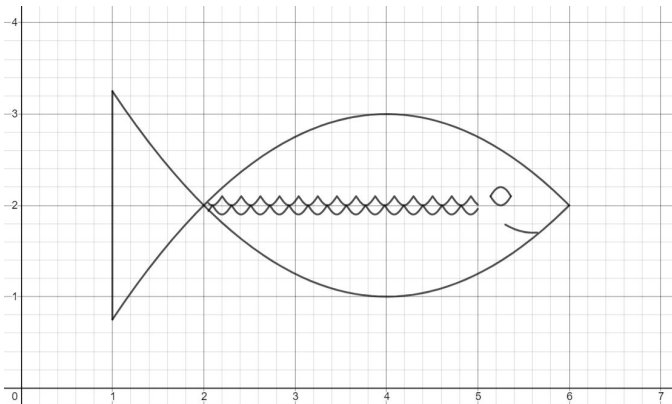
$$y = |\sin(x)|$$

$$y = -|\sin(x)|$$

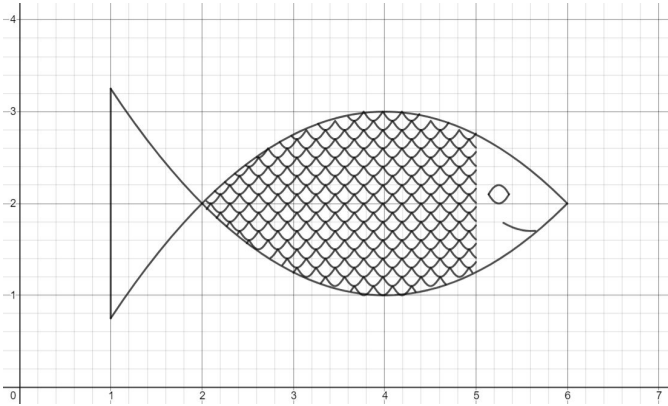
**Exercise.** Previously, you drew a fish using parabolas. Now, create a layer of scales on it, using a function of the form  $y = -A|\sin(x)| + b$ .



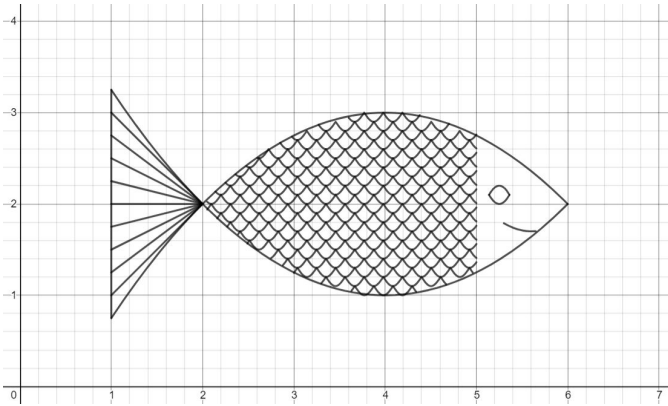
**Exercise.** Now, create a second layer of scales, using a function of the form  $y = -A|\sin(x - a)| + b$ . The peaks of the first layer should line up with the valleys of the second layer.



**Exercise.** Continue making layers of scales until the fish is completely scaled.



**Exercise.** Lastly, use lines to create spines in the tail of the fish.



**Challenge.** Try to draw other scaled creatures, such as a snake!